Chapter 16
Location and Logistics

Sibel A. Alumur, Bahar Y. Kara, and M. Teresa Melo

Abstract Facility location decisions play a critical role in designing logistics networks. This chapter provides some guidelines on how location decisions and logistics functions can be integrated into a single mathematical model to optimize the configuration of a logistics network. This will be illustrated by two generic models, one supporting the design of a forward logistics network and the other addressing the specific requirements of a reverse logistics network. Several special cases and extensions of the two models are discussed and their relation with the scientific literature is described. In addition, some interesting applications are outlined that demonstrate the interaction of location and logistics decisions. Finally, new research directions and emerging trends in logistics network design are provided.

Keywords Forward logistics network design • Reverse logistics network design • Models • Applications

16.1 Introduction

Logistics network design (LND) and facility location decisions are closely interrelated. The latter are prompted by the need either to build a new logistics network or to re-design a network that is already in place. When a company enters new markets or grows into new product segments, a new logistics network has to be designed. However, “green field” projects are less frequent compared with re-design initiatives. Changing market and business conditions compel a company to modify
the physical structure of its logistics network from time to time. Major drivers of network re-design projects comprise variations in the demand pattern and its spatial distribution as well as increased cost pressure and service requirements. Moreover, mergers, acquisitions, and strategic alliances also trigger the expansion or reconfiguration of a logistics network in order to exploit the benefits and synergies of integrating the acquired operations. Typically, re-design activities take the form of opening new facilities (e.g., to be closer to new markets) and closing existing facilities (e.g., to consolidate operations). As highlighted by Ballou (2001) and Harrison (2004), well-conceived re-design decisions can result in a 5–15% reduction of the overall logistics costs, with 10% being often achieved.

The (re-)design of a logistics network is a complex undertaking. It concerns not only determining the number, size, and capacity of facilities (e.g., plants and warehouses) to be operated but it also involves planning and integrating a manifold of logistics functions that such facilities will perform. These functions range from procurement of raw materials, transformation of these materials into semi-finished and end products, and the delivery of finished products to customers through one or several distribution stages. Depending on the industrial context, strategic decisions may also concern the collection and recovery of product returns.

This chapter provides a holistic approach to strategic network planning by integrating facility location decisions with decisions relevant to the configuration of a logistics network. The integrated view will be illustrated by two general modeling frameworks for designing forward and reverse logistics networks.

The remainder of the chapter is organized as follows. Section 16.2 presents a comprehensive model for logistics networks with forward flows. Due to its generic features, the model applies to a wide range of situations. Its relation with other models proposed in the literature is established and extensions are discussed. Section 16.3 focuses on reverse logistics network design (RLND) and introduces a generic mathematical formulation for the design of a multi-purpose reverse logistics network. Furthermore, some special cases and extensions of the proposed model are presented. Section 16.4 addresses various representative applications of forward and reverse LND problems from different areas. Finally, in Sect. 16.5 future research directions are discussed.

16.2 A General Logistics Network Design Model

We introduce a base model that captures the main features of an LND problem. The starting point is either a potential framework for a new network structure or an existing network whose physical structure is to be re-designed. To this end, a general network typology, as depicted in Fig. 16.1, is considered. Any number of facility layers and any system of transportation channels can be modeled. The network entities are categorized in so-called selective and non-selectable facilities. The former group includes a set of facilities already in place, that could be closed, and a set of potential locations for establishing new facilities. In contrast, non-selectable
facilities comprise facilities that are not subject to location decisions. Typically, such facilities include suppliers as well as existing plants and/or warehouses that should be maintained. In addition, customer zones are viewed as special members of this set as they have demand requirements for multiple commodities. As shown in Fig. 16.1, no restrictions are imposed on the availability of transportation channels for the flow of materials through the network. In particular, direct commodity flows from upstream sources to customer zones (or to facilities not immediately below in the hierarchy) are possible as well as flows between facilities in the same echelon. In this rather general network typology, procurement, production, distribution, and customer service decisions are to be made along with facility location and sizing decisions. The mathematical model in Sect. 16.2.2 captures the aforementioned features. The required notation is first introduced in Sect. 16.2.1. Several special cases and extensions are discussed in Sect. 16.2.3.

### 16.2.1 Notation and Definition of Decision Variables

Table 16.1 introduces the index sets that are used in the base model. In addition to the various types of network entities, also multiple commodities are considered, ranging from raw materials and intermediate products to finished goods. Moreover, different kinds of resources may be available for manufacturing and handling commodities.

Table 16.2 describes input parameters related to logistics operations. Multi-stage production processes can be taken into account through bills-of-materials (BOMs). In this case, the relationships between components and parent items are defined...
Table 16.1  Index sets

<table>
<thead>
<tr>
<th>Symbol</th>
<th>Description</th>
<th>Index symbol</th>
</tr>
</thead>
<tbody>
<tr>
<td>N</td>
<td>Set of potential locations for new facilities</td>
<td>i</td>
</tr>
<tr>
<td>E</td>
<td>Set of existing facilities that could be closed</td>
<td>i</td>
</tr>
<tr>
<td>I</td>
<td>Set of selectable facilities, $I = N \cup E$</td>
<td>i</td>
</tr>
<tr>
<td>J</td>
<td>Set of non-selectable locations (e.g., customer zones)</td>
<td>$j, j'$</td>
</tr>
<tr>
<td>L</td>
<td>Set of all entities, $L = I \cup J$</td>
<td>$\ell, \ell'$</td>
</tr>
<tr>
<td>P</td>
<td>Set of products</td>
<td>p, q</td>
</tr>
<tr>
<td>$M, H$</td>
<td>Set of manufacturing, resp. handling resources</td>
<td>m, h</td>
</tr>
</tbody>
</table>

Table 16.2  Logistics parameters

<table>
<thead>
<tr>
<th>Symbol</th>
<th>Description</th>
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<tbody>
<tr>
<td>$d_{\ell p}$</td>
<td>Demand of location $\ell \in L$ for product $p \in P$ (typically, $d_{ip} = 0$ for $i \in I$)</td>
</tr>
<tr>
<td>$\alpha_{\ell qp}$</td>
<td>Number of units of product $q \in P$ required to manufacture one unit of product $p \in P$ ($q \neq p$) at facility $\ell \in L$</td>
</tr>
<tr>
<td>$\mu_{\ell mp}$</td>
<td>Number of units of resource $m \in M$ required to manufacture one unit of product $p \in P$ at facility $\ell \in L$</td>
</tr>
<tr>
<td>$\hat{\lambda}<em>{\ell hp}, \tilde{\lambda}</em>{\ell hp}$</td>
<td>Number of units of resource $h \in H$ required to handle one unit of product $p \in P$ upon its arrival at, resp. shipment from, facility $\ell \in L$</td>
</tr>
<tr>
<td>$KM_m, KH_h$</td>
<td>Capacity of manufacturing resource $m \in M$, resp. handling resource $h \in H$</td>
</tr>
<tr>
<td>$EM_m, EH_h$</td>
<td>Maximum increase in capacity of manufacturing resource $m \in M$, resp. handling resource $h \in H$</td>
</tr>
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</table>

by given parameters. Capacities of service facilities are modeled in a general way through manufacturing and handling resources. Three different relation types are considered. In a many-to-one relationship, several resources are available at the same facility. Some resources may be product-specific (e.g., a machine dedicated to a given item) while others may be shared by multiple commodities (e.g., production line or order picking system). A one-to-one association corresponds to the classical way of modeling capacity in facility location models (e.g., storage space in a warehouse). One-to-many relationships can also be modeled, although these are less common. This could be the case, for example, of a team of experts responsible for several production lines in different facilities. Resource availability can be increased at additional expense, e.g., through overtime work or leasing extra storage space. Resource consumption is described by specific parameters. In the case of handling resources, the same type of equipment (e.g., forklift truck) may be required with different intensity to unload incoming goods at a facility and load goods to be shipped from the same facility.

Table 16.3 summarizes all facility and logistics costs. Facility costs are related to establishing new facilities and closing existing facilities, and typically reflect economies of scale. In addition, facility operating costs represent, for example, business overhead costs such as staff and security costs. Logistics costs are incurred for purchasing items from external sources (e.g., procurement of raw materials),
Table 16.3 Cost parameters

<table>
<thead>
<tr>
<th>Symbol</th>
<th>Description</th>
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</thead>
<tbody>
<tr>
<td>$FC_i$</td>
<td>Fixed setup cost of establishing a new facility in location $i \in N$</td>
</tr>
<tr>
<td>$SC_i$</td>
<td>Fixed cost of closing existing facility $i \in E$</td>
</tr>
<tr>
<td>$OC_\ell$</td>
<td>Fixed cost of operating facility $\ell \in L$</td>
</tr>
<tr>
<td>$BC_{\ell p}$</td>
<td>Unit cost of buying product $p \in P$ at facility $\ell \in L$ from an external source</td>
</tr>
<tr>
<td>$PC_{\ell p}$</td>
<td>Unit cost of producing product $p \in P$ at facility $\ell \in L$</td>
</tr>
<tr>
<td>$TC_{\ell \ell' p}$</td>
<td>Unit cost of transporting product $p \in P$ from facility $\ell \in L$ to facility $\ell' \in L$ ($\ell \neq \ell'$)</td>
</tr>
<tr>
<td>$MC_m$, $HC_h$</td>
<td>Unit cost of expanding manufacturing resource $m \in M$, resp. handling resource $h \in H$</td>
</tr>
<tr>
<td>$DC_{\ell p}$</td>
<td>Unit penalty cost for not serving demand of facility $\ell \in L$ for product $p \in P$</td>
</tr>
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Table 16.4 Decision variables

<table>
<thead>
<tr>
<th>Symbol</th>
<th>Description</th>
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<tbody>
<tr>
<td>$y_i$</td>
<td>1 if the selectable facility $i \in I$ is operated, 0 otherwise</td>
</tr>
<tr>
<td>$s_{\ell p}$</td>
<td>Quantity of product $p \in P$ purchased at facility $\ell \in L$ from an external source</td>
</tr>
<tr>
<td>$z_{\ell p}$</td>
<td>Quantity of product $p \in P$ manufactured at facility $\ell \in L$</td>
</tr>
<tr>
<td>$x_{\ell \ell' p}$</td>
<td>Quantity of product $p \in P$ shipped from facility $\ell \in L$ to facility $\ell' \in L$ ($\ell \neq \ell'$)</td>
</tr>
<tr>
<td>$w_m$, $\overline{w}_h$</td>
<td>Number of extra capacity units of manufacturing resource $m \in M$, resp. handling resource $h \in H$</td>
</tr>
<tr>
<td>$u_{\ell p}$</td>
<td>Quantity of unsatisfied demand of location $\ell \in L$ for product $p \in P$</td>
</tr>
</tbody>
</table>

for manufacturing commodities, and for distributing multiple products through the network. The latter costs may also include charges for handling goods at the source facility and at the destination facility (e.g., order picking and warehousing costs). Furthermore, additional costs are considered for resource expansion. Penalty costs are also incurred for failing to meet customer demand. These costs represent the additional expense for outsourcing unfilled demand.

Finally, strategic decisions on facility location and logistics operations are ruled by the variables in Table 16.4.

16.2.2 A Mixed-Integer Linear Programming Model

Under the assumption that all inputs are known non-negative quantities, the logistics network (re-)design problem can be formulated as a mixed-integer linear program (MILP) as follows.

The objective function (16.1) describes the aim of the decision-making process, namely to identify the network configuration with the least total cost. To this end, fixed costs associated with opening, closing, and operating facilities are considered. The latter include a fixed cost term for maintaining facilities that are not subject to
Variable costs account for resource expansion and for material procurement, production, and distribution. In addition, penalty costs are incurred to unfilled demand.

\[(P_1) \text{ Minimize } \sum_{i \in N} FC_i \cdot y_i + \sum_{i \in E} SC_i \cdot (1 - y_i) + \sum_{i \in I} OC_i \cdot y_i + \sum_{j \in J} OC_j + \sum_{m \in M} MC_m \cdot w_m \]

\[+ \sum_{h \in H} HC_h \cdot \bar{w}_h + \sum_{\ell \in L} \sum_{p \in P} BC_{\ell p} \cdot s_{\ell p} + \sum_{\ell \in L} \sum_{p \in P} PC_{\ell p} \cdot z_{\ell p} \]

\[+ \sum_{\ell \in L} \sum_{p \in P} \sum_{\ell' \in L \setminus \{\ell\}} \sum_{p \in P} TC_{\ell' p} \cdot x_{\ell' p} + \sum_{\ell \in L} \sum_{p \in P} DC_{\ell p} \cdot u_{\ell p} \quad (16.1)\]

subject to \[
\sum_{\ell' \in L \setminus \{\ell\}} x_{\ell' p} + z_{\ell p} = \\
\sum_{q \in P} \alpha_{\ell pq} \cdot z_{pq} + \sum_{\ell' \in L \setminus \{\ell\}} x_{\ell' p} + d_{\ell p} - u_{\ell p}, \quad \ell \in L, \ p \in P
\]

\[\sum_{\ell \in L} \sum_{p \in P} \mu_{\ell mp} \cdot z_{\ell p} \leq KM_m + w_m, \ m \in M \quad (16.2)\]

\[\sum_{\ell \in L} \sum_{p \in P} \lambda_{\ell hp} \cdot s_{\ell p} + \sum_{\ell \in L} \sum_{\ell' \in L \setminus \{\ell\}} \sum_{p \in P} (\lambda_{\ell hp} + \lambda_{\ell' hp}) \cdot x_{\ell' p} \leq KH_h + \bar{w}_h, \ h \in H \quad (16.3)\]

\[0 \leq w_m \leq EM_m, \ m \in M \quad (16.4)\]

\[0 \leq \bar{w}_h \leq EH_h, \ h \in H \quad (16.5)\]

\[0 \leq u_{\ell p} \leq d_{\ell p}, \ \ell \in L, \ p \in P \quad (16.6)\]

\[0 \leq s_{ip} \leq s_i \cdot y_i, \ i \in I, \ p \in P \quad (16.7)\]

\[0 \leq z_{ip} \leq z_i \cdot y_i, \ i \in I, \ p \in P \quad (16.8)\]

\[0 \leq x_{ip} \leq x_i \cdot y_i, \ i \in I, \ \ell \in L \setminus \{i\}, \ p \in P \quad (16.9)\]

\[0 \leq x_{i\ell p} \leq x_i \cdot y_i, \ i \in I, \ \ell \in L \setminus \{i\}, \ i \in I, \ p \in P \quad (16.10)\]

\[s_{jp} \geq 0, \ z_{jp} \geq 0, \ x_{jj'} \geq 0, \ j, j' \in J \ (j \neq j'), \ p \in P \quad (16.11)\]

\[y_i \in \{0, 1\}, \ i \in I. \quad (16.12)\]

Constraints (16.2) are the usual flow balance equations. The inbound flow of an item to a facility consists of procuring or producing the item at the facility or
receiving it from other locations. The outbound flow results from using the product as a raw material to manufacture other commodities, distributing the item to other facilities, or serving demand in case the location is a customer zone. Inequalities (16.3), resp. (16.4), guarantee that the usage of manufacturing, resp. handling, resources does not exceed the available capacity. Constraints (16.5)–(16.6) stipulate that capacity expansions must be within given limits. Constraints (16.7) rule the maximum amount of unsatisfied demand. Inequalities (16.8)–(16.11) ensure that procurement, production, and distribution activities only occur at operating facilities. A sufficiently large constant $M$ is used in these constraints which can be adjusted depending on each specific situation. Typically, $M$ is replaced by the maximum quantity that can be processed by a facility with respect to all product types. Finally, constraints (16.12) are non-negativity conditions for the logistics operations in non-selectable locations, while constraints (16.13) are binary requirements for the location variables.

Although the above problem is NP-hard, being a generalization of the simple plant location problem (see Krarup and Pruzan 1983), Melo et al. (2008) could solve medium and large-sized randomly generated instances to optimality with general purpose optimization software within reasonable time. To analyze the quality of the MILP formulation, the linear relaxation bound was also compared with the optimal solution of the tested instances. In general, a relatively small gap could be observed. These findings have important practical implications, since managers often need to base their decisions on the results of several scenarios. Hence, for a company to be able to perform “what-if” analysis and thereby identify good quality (or even optimal) solutions with an acceptable level of computational effort is a major step towards better decision support.

### 16.2.3 Special Cases and Model Extensions

Historically, researchers have focused relatively early on the design of distribution systems with at most two facility layers (e.g., plants and warehouses). In these simple networks, decisions were mostly confined to facility location and distribution operations. The contribution by Geoffrion and Graves (1974) is such an example. In recent years, the trend has been towards the development of more comprehensive models that integrate location decisions with supplier selection, production planning, technology acquisition, inventory management, transportation mode selection, and vehicle routing, just to mention some important logistics functions considered in this area (see Melo et al. 2009 for a comprehensive review). In many cases, the proposed models combine strategic decisions (e.g., location and capacity choices) with tactical decisions (e.g., inventory and transportation management) or even operational decisions (e.g., vehicle routing). Usually, the interplay of different planning levels can only be captured at the cost of increased model complexity. This will be illustrated in Sect. 16.4 by three applications.
The generic formulation \( (P_1) \) comprises some of the aforementioned features and it can also be adapted or extended to include further aspects relevant to LND. For example, it is easy to add single-sourcing requirements to \( (P_1) \) to ensure that the demand of each customer zone for a particular product is entirely satisfied from a unique facility. A straightforward extension of \( (P_1) \) is also to embed the (re-)design of a logistics network in a multi-period planning horizon. Such a setting is meaningful since the establishment of new facilities is typically a long-term project involving time-consuming activities and requiring the commitment of substantial capital resources. In this case, strategic decisions can be constrained by the budget available in each time period. Logistics decisions will be in turn impacted by the location choices. Fleischmann et al. (2006) and more recently Correia et al. (2013) included this feature in their dynamic network design models.

A multi-period setting is also appropriate for planning the re-design of a logistics network that is already in place. In this context, existing facilities may have their capacities expanded, reduced or even moved to new sites over several time periods as illustrated in Fig. 16.2 (the bars in the figure next to the facilities indicate their size). In turn, new facilities can be established through successive sizing. A gradual transfer of production and/or storage capacities from existing locations to new sites ensures a smooth implementation of relocation plans and avoids logistics operations from being disrupted. Melo et al. (2006, 2012, 2014) proposed several models and heuristics for this special form of network re-design.

In the mathematical model \( (P_1) \) all inputs (i.e., logistics and cost parameters) are taken as known quantities. As noted by Melo et al. (2009), most of the research dedicated to LND problems focuses on deterministic formulations. This is explained by the complexity posed by many of these problems and the serious computational hurdle that arises when the problem size becomes large. In the last two decades, increasing attention has been given to the development of new models that incorporate the uncertainties inherent to decision-making in LND (see Klibi et al. 2010). This is the case, for example, of the multi-echelon LND problem addressed by Santosso et al. (2005). Uncertainty is captured with respect to supply and demand quantities, resource capacities, and processing as well as transportation costs. Recently, Huang and Goetschalckx (2014) developed a scenario planning approach for a similar problem focusing on solution robustness. The goal is to obtain...
a network configuration such that the solution values do not substantially vary over different scenarios. Several authors also included stochastic problem characteristics in a multi-period setting such as Aghezzaf (2005), Pan and Nagi (2010), and Nickel et al. (2012).

A further relevant aspect in strategic network design is the integration of location decisions with inventory management. Demand uncertainty and risk pooling play an important role in this context. Inventory decisions concern working inventories at storage locations (i.e., the amounts of products that have been ordered from suppliers but not yet requested by customers) and safety stocks. The latter are intended as a buffer against stockouts during ordering lead times. Shen (2005), Ozsen et al. (2009), and Shu (2010) study the trade-off between inventory, transportation, and fixed costs to locate warehouses and allocate customers. Combining inventory management and location decisions into a single model often results in mixed-integer non-linear programming formulations that can only be solved for small problem instances. Recently, Tancrez et al. (2012) developed a heuristic procedure that is able to solve large-scale multi-echelon location-inventory problems comprising plants, distribution centers, and customers.

Finally, the growth in globalization has led to the emergence of global supply chains, that is, worldwide networks of suppliers, manufacturers, distribution centers, and retailers. Consequently, the integration of financial considerations with location and logistics decisions has gained increasing importance in network design. Financial factors comprise, among others, taxes, duties, tariffs, exchange rates, and transfer prices. Meixell and Gargeya (2005) discuss various contributions in this area while Wilhelm et al. (2005) propose a comprehensive model for the design of a logistics network under the North American Free Trade Agreement (NAFTA).

### 16.3 A General Reverse Logistics Network Design Model

Reverse logistics refers to all operations involved in the return of products and materials from a point of use to a point of recovery or proper disposal. The purpose of recovery is to recapture value through options such as reusing, repairing, refurbishing, remanufacturing, and recycling. Reverse logistics includes the management of the return of end-of-use or end-of-life products as well as defective and damaged items, or packaging materials, containers, and pallets.

Major driving forces behind reverse logistics activities include economical factors, legislations, and environmental consciousness. As stated by De Brito and Dekker (2004), companies become active in reverse logistics because they can make a profit and/or because they are forced to focus on such functions, and/or because they feel socially motivated. These factors are usually intertwined. For example, a company can be compelled to reuse a certain percentage of components in order to achieve a recovery target set by the legislation. This will lead to a decrease in the cost of purchasing components and in waste generation. Jayaraman and Luo (2007) suggest that proper management of reverse logistics operations can lead to greater
profitability and customer satisfaction, and at the same time be beneficial to the environment.

Many actors are involved in the design and operation of a reverse logistics network. Even though extended producer responsibilities present in the legislations in various countries give the responsibility of recovering used products to original equipment manufacturers, governments need to establish the necessary infrastructure. Responsibilities can be shared among different parties, such as producers, distributors, third-party logistics providers, or municipalities, in designing and operating the reverse logistics networks.

In a reverse logistics network, end-of-life or end-of-use products can be generated at private households and at commercial, industrial, and institutional sources, which are referred to as generation points. Products are usually collected at special storage facilities called collection or inspection centers. Products are then sent for proper recovery through reusing, repairing, refurbishing, remanufacturing, or recycling. Inspected or recovered products and components can then be sold to suppliers, to (re)manufacturing facilities, or to customers in the secondary market. A generic reverse logistics network is depicted in Fig. 16.3.

Unlike forward logistics networks, where demand occurs at the lower echelon facilities, in reverse networks demand (for recovery) arises at the upper echelon facilities. However, a reverse logistics network is not a mirror image of a forward network. In addition to the typical forward supply chain actors, different actors and facilities are involved in reverse logistics networks, such as disposers, remanufacturers, and the secondary market. Moreover, unlike forward networks, which are mostly driven by economical factors, there are further factors motivating the establishment of reverse logistics networks such as environmental laws.

In Sect. 16.3.2, a generic mathematical formulation for the design of a multipurpose reverse logistics network is presented. The required notation and the
decision variables are first defined in Sect. 16.3.1. Some special cases and possible extensions of the proposed model are additionally discussed in Sect. 16.3.3.

### 16.3.1 Notation and Definition of Decision Variables

The notation used in the generic RLND model is analogous to the notation introduced in Sect. 16.2.1 for the forward LND model. Similar to the forward network design problem, multiple commodities are considered in the configuration of the reverse logistics network. These are represented by the set $P$, which may include used, inspected, repaired, or refurbished products, components, or raw materials. In order to represent a different state (inspected, repaired, refurbished, etc.) of a certain item, a different product type needs to be defined within the set $P$. Table 16.5 describes all index sets that are required for modeling the RLND problem.

The set of available recovery options may include conventional options, such as repair, refurbish, and recycle as well as other options such as inspection, disassembly, selling to suppliers, to the secondary market or to external (re)manufacturing facilities, and disposal. Even though the latter options may not be regarded as recovery alternatives, in order to provide a generic model incorporating all the decisions present in real-life reverse logistics networks, they are included in the set $R$. Observe that some recovery options may be operated by third-party logistics providers. These external facilities belong to the set $J_r$. Moreover, it is assumed that generation points are also included in this set of non-selectable facilities.

Table 16.6 introduces the required parameters. Transitions between the stages of products and reverse BOMs are taken into account by the parameter $\beta$. For example, a damaged product can be converted into a repaired product through the recovery option repair, or a used product can be disassembled into its components at a disassembly facility. Each recovery option has a given capacity which can be expanded at selectable facilities. Revenues may be obtained through some recovery options, e.g., by selling products or components to recycling facilities, to the

<table>
<thead>
<tr>
<th>Table 16.5</th>
<th>New index sets</th>
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</thead>
<tbody>
<tr>
<td>Symbol</td>
<td>Description</td>
</tr>
<tr>
<td>$R$</td>
<td>Set of recovery options (e.g., repair, refurbish, recycle)</td>
</tr>
<tr>
<td>$N_r$</td>
<td>Set of potential locations for recovery option $r \in R$</td>
</tr>
<tr>
<td>$E_r$</td>
<td>Set of existing facilities with recovery option $r \in R$</td>
</tr>
<tr>
<td>$I_r$</td>
<td>Set of selectable facilities with recovery option $r \in R$, $I_r = N_r \cup E_r$</td>
</tr>
<tr>
<td>$J_r$</td>
<td>Set of non-selectable locations with recovery option $r \in R$ (e.g. secondary market, disposal)</td>
</tr>
<tr>
<td>$L$</td>
<td>Set of all locations, $L = \bigcup_{r \in R} (I_r \cup J_r)$</td>
</tr>
</tbody>
</table>
Table 16.6  New parameters

<table>
<thead>
<tr>
<th>Symbol</th>
<th>Description</th>
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<tbody>
<tr>
<td>$g_{lp}$</td>
<td>Amount of product $p \in P$ generated at location $l \in L$</td>
</tr>
<tr>
<td>$\beta_{lpq}$</td>
<td>Number of units of product $p \in P$ obtained by processing one unit of product $q \in P$ ($q \neq p$) using recovery option $r \in R$</td>
</tr>
<tr>
<td>$KR_{rl}$</td>
<td>Capacity of recovery option $r \in R$ at location $l \in L$</td>
</tr>
<tr>
<td>$ER_{ri}$</td>
<td>Maximum increase in capacity for recovery option $r \in R$ at location $i \in I_r$</td>
</tr>
<tr>
<td>$RT_{rp}$</td>
<td>Recovery target for product $p \in P$ with recovery option $r \in R$</td>
</tr>
<tr>
<td>$RE_{rlp}$</td>
<td>Revenue from recovering one unit of product $p \in P$ with recovery option $r \in R$ at location $l \in L$ (e.g., revenue from recycling or from the secondary market)</td>
</tr>
<tr>
<td>$RC_{rlp}$</td>
<td>Cost of recovering one unit of product $p \in P$ with recovery option $r \in R$ at location $l \in L$</td>
</tr>
<tr>
<td>$FC_{ri}$</td>
<td>Fixed setup cost of establishing recovery option $r \in R$ at location $i \in N_r$</td>
</tr>
<tr>
<td>$SC_{ri}$</td>
<td>Fixed cost of closing recovery option $r \in R$ at existing facility $i \in E_r$</td>
</tr>
<tr>
<td>$OC_{rl}$</td>
<td>Fixed cost of operating recovery option $r \in R$ at location $l \in L$</td>
</tr>
<tr>
<td>$EC_{ri}$</td>
<td>Unit cost of expanding capacity of recovery option $r \in R$ at location $i \in I_r$</td>
</tr>
</tbody>
</table>

Table 16.7  New decision variables

<table>
<thead>
<tr>
<th>Symbol</th>
<th>Description</th>
</tr>
</thead>
<tbody>
<tr>
<td>$y_{ri}$</td>
<td>1 if recovery option $r \in R$ is operated at the selectable facility $i \in I_r$, 0 otherwise</td>
</tr>
<tr>
<td>$v_{rlp}$</td>
<td>Amount of product $p \in P$ recovered with recovery option $r \in R$ at location $l \in L$</td>
</tr>
<tr>
<td>$w_{ri}$</td>
<td>Number of extra capacity units established for recovery option $r \in R$ at location $i \in I_r$</td>
</tr>
</tbody>
</table>

Finally, Table 16.7 describes the decision variables. The RNLD model also uses the flow variables $x$ introduced in Table 16.4.

### 16.3.2 A Mixed-Integer Linear Programming Model

With the notation introduced in the previous section, the reverse logistics network (re-)design problem can be formulated as an MILP as follows. The objective function (16.14) maximizes the total profit. It sums the revenues obtained from various recovery options (e.g., by sending products to recycling facilities, by selling products to the secondary market) and subtracts the total cost of establishing and operating the network. The latter comprises the cost of recovering products at facilities, setting up new recovery options at facilities, closing existing recovery options, operating new and existing recovery options at facilities, transporting products, and expanding the capacities of recovery options. Observe that a fixed
cost term is also included in (16.14) to account for the operation of non-selectable facilities.

Equalities (16.15) are the flow balance constraints. For each location and product, the total inflow comprises the amount of product generated at that location, the total amount of product obtained after processing various items, and the total amount of product shipped to this location from other locations. The total inflow is equal to the total outflow which includes the total amount of product recovered at that location and the total amount of product shipped to other locations. Constraints (16.16) ensure that the recovery target for each product category and recovery option is met. Recovery targets are usually stipulated by legislations for different types of recovery options. Inequalities (16.17)–(16.19) are the capacity constraints. Constraints (16.17) guarantee that the total amount of recovered products at the selectable facilities does not exceed the total capacity. Similar conditions are set at non-selectable facilities by inequalities (16.18). Constraints (16.19) restrict the expansion of capacity at selectable facilities to be within given limits. Similar to the forward LND model, constraints (16.20)–(16.21) impose that products can only be shipped from operated facilities. Lastly, conditions (16.22)–(16.24) set the domains of the decision variables.

\[(P_2) \quad \text{Maximize} \quad \sum_{r \in R} \sum_{\ell \in L} \sum_{p \in P} \left( RE_{r \ell p} v_{r \ell p} - \sum_{r \in R} \sum_{\ell \in L} \sum_{p \in P} RC_{r \ell p} v_{r \ell p} - \sum_{r \in R} \sum_{i \in N_r} FC_{ri} y_{ri} - \sum_{r \in R} \sum_{i \in E_r} SC_{ri} (1 - y_{ri}) - \sum_{r \in R} \sum_{i \in I_r} OC_{ri} y_{ri} - \sum_{r \in R} \sum_{j \in J_r} OC_{rj} \right) \]

subject to

\[
g_{tp} + \sum_{r \in R} \sum_{q \in P} \beta_{rqp} v_{r tp} + \sum_{\ell' \in L \setminus \{\ell\}} x_{\ell' \ell p} = \sum_{r \in R} v_{r \ell p} + \sum_{\ell' \in L \setminus \{\ell\}} x_{\ell' \ell p}, \quad \ell \in L, \quad p \in P \]

\[
\sum_{\ell \in L} v_{r \ell p} \geq RT_{rp}, \quad r \in R, \quad p \in P \]

\[
\sum_{p \in P} v_{ri p} \leq KR_{ri} y_{ri} + w_{ri}, \quad r \in R, i \in I_r \]

\[
\sum_{p \in P} v_{rjp} \leq KR_{rj}, \quad r \in R, \quad j \in J_r \]

\[
0 \leq w_{ri} \leq ER_{ri} y_{ri}, \quad r \in R, \quad i \in I_r \]
\begin{align}
0 & \leq x_{i\ell p} \leq M \sum_{r \in R} y_{ri}, \quad i \in \bigcup_{r \in R} I_r, \quad \ell \in L \setminus \{i\}, \quad p \in P \\
0 & \leq x_{iip} \leq M \sum_{r \in R} y_{ri}, \quad \ell \in L \setminus \{i\}, \quad i \in \bigcup_{r \in R} I_r, \quad p \in P \\
x_{jj'p} & \geq 0, \quad j, j' \in \bigcup_{r \in R} J_r \ (j \neq j'), \quad p \in P \\
v_{r\ell p} & \geq 0, \quad r \in R, \quad \ell \in L, \quad p \in P \\
y_{ri} & \in \{0, 1\}, \quad r \in R, \quad i \in I_r.
\end{align}

The proposed model is generic in the sense that it includes multiple types of products and components at different stages (inspected, repaired, refurbished, etc.). Moreover, it considers reverse BOMs and transitions between the stages of products through various recovery options. The problem is modeled with a profit oriented objective function accounting for the revenues from different recovery options in addition to costs.

In terms of problem complexity, the above RLND model has similar attributes to the forward network design problem ($P_1$). Moreover, general purpose optimization software (e.g., CPLEX or Gurobi) can be used to solve ($P_2$). However, for large-sized instances there may be a need for customized algorithms and heuristics.

### 16.3.3 Special Cases and Model Extensions

The generic model ($P_2$) can be easily tailored to different applications. A reverse logistics network design application for the collection and recovery of waste electrical and electronic equipment is detailed in Sect. 16.4.4.

The term closed-loop supply chain refers to a network comprising both forward and reverse flows. Figure 16.4 depicts the structure of such a network. The cost of processing a return flow in a supply chain designed by considering only forward flows can be much higher than processing a flow in the forward direction. Thus, supply chain networks that include flows in the reverse direction should be designed by integrating forward and reverse logistics activities. The models introduced in Sects. 16.2.2 and 16.3.2 are readily extendible to the design of closed-loop supply chains. The interested reader is referred to Krikke et al. (2003), Easwaran and Üster (2009), and Salema et al. (2010) for exemplary studies determining the locations of facilities within closed-loop supply chain networks.

As emphasized in Sect. 16.2.3, the dynamic nature of the (re-)design problem should not be disregarded. Multi-period models in RLND were proposed, for example, by Lee and Dong (2009), Salema et al. (2010), and Alumur et al. (2012).
A distinguishing feature of RLND problems is that various sources of uncertainty in supply arise at the upper echelon facilities (e.g., uncertainty in the amount and in the quality of returned products). There are some studies addressing uncertainty issues in the context of RLND such as Realf et al. (2004), Listesi and Dekker (2005), Listesi (2007), Salema et al. (2007), El-Sayed et al. (2010), and Fonseca et al. (2010).

As discussed at the beginning of Sect. 16.3, major driving forces in reverse logistics networks include not only economical factors, but also legislations and environmental consciousness. Thus, in addition to the actors involved in forward logistics networks, actors such as municipalities, foundations, third-party logistics providers, and disposers, are involved in designing and operating reverse logistics networks. Multiple actors lead to decision problems with multiple objectives. Even though there are some studies that consider the multi-objective nature of this design problem (e.g., Pati et al. 2008, Fonseca et al. 2010, Tari and Alumur 2014), this issue requires further attention.

For other extensions and special cases on RLND, the interested reader is referred to the reviews by Fleischmann et al. (2004), Bostel et al. (2005), Akçalı et al. (2009), and Aras et al. (2010).

### 16.4 Applications

The aim of this section is to demonstrate the richness in LND through presenting applications from various areas including organ transportation in addition to classical areas. The general form of the models described in Sects. 16.2 and 16.3
allows them to be applied to an LND problem of a manufacturer as well as of a logistics service provider under appropriate set, parameter, and variable definitions.

In this section, four applications from different sectors are discussed. Section 16.4.1 presents the network design problem of a global beverage company. Many companies utilize logistics service providers in their distribution networks. In Sect. 16.4.2 an application from this area is provided. Section 16.4.3 is devoted to an atypical application in LND arising in organ transportation. The problem has additional features resulting from the nature of the good being transported. Finally, Sect. 16.4.4 illustrates an application for waste electrical and electronic equipment.

16.4.1 Logistics Network Design of a Beverage Company

Beverage companies usually operate bottling factories in which the required materials are mixed, bottled, and then packaged to be shipped to end users. Global companies usually need to import some of the input materials, like flavors and syrups, to guarantee the same quality worldwide. Moreover, ingredients may also be provided by local suppliers. Thus, inbound logistics involves both international and national shipments to the manufacturing plant. In turn, the outbound flow from the plant comprises bottled and packaged beverages ready to consume. The flow of end products may also be targeted at neighboring countries, thus involving again national and international shipping. The schematic representation of the logistics network, which is a specialized version of Fig. 16.1, is given in Fig. 16.5.

The main decisions in this LND problem include the location of new distribution centers (DCs) and the choice of transportation channels for the inbound and outbound flows of these DCs. As can be seen from Fig. 16.5, the manufacturer may choose to operate additional DCs closer to the customs area to ease the overall customs process. Certain beverages are not produced in every country. Thus, there is a bottled beverage flow from the customs area towards DCs for those products that are not manufactured in a country. Shipments to international customers (via the customs) mainly consist of products that are produced in the local country and they will constitute the in-country product flow in the LND problems of other countries.

Observe here that, in addition to finding the locations of DCs and deciding on the transportation structures to use, the LND problem also includes routing decisions for deliveries to the customers (see the dashed lines in Fig. 16.5). Typically, a global beverage company resorts to logistics service providers to handle the distribution of orders to end users. The service provider operates its own logistics network, which will be detailed in the next subsection. Apart from location and routing decisions, a typical beverage company also questions:

- the level of inventories at the DCs,
- the need for consolidation; some examples include consolidation on the route and consolidation at the facility,
16.4.2 Logistics Network Design of a Logistics Service Provider Company

LND is a crucial problem for logistics service provider (LSP) companies since they offer warehousing and transportation services to multiple manufacturers having specific requirements. A typical LSP company generally operates based on yearly contracts, each defining the level of integration to be provided to the customer. This can range from basic services, which mainly handle the transportation aspect of the overall distribution network, to integrated logistics activities, which can even include packaging, labeling, and customs clearance type of services. The design of the network of such a company is, of course, influenced by the level of integration. Nevertheless, a typical LSP usually operates several DCs and the
number of DCs is based on the geographical span and on the promised service levels. Since the logistics network of the service provider company does not include inbound shipments towards production plants, a generic network is composed of production facilities, DCs, and customers (cf. Fig. 16.1). The main decisions to be made in the LND problem include the location of DCs and the choice of appropriate transportation structures.

Consolidation is a crucial aspect in the distribution network of an LSP company. Especially in small geographical regions, say in urban areas, companies try to consolidate customer orders into full truckload shipments. As a result, delivery and/or collection vehicles serve many customers on each route they travel.

Typically, an LSP company operates a few DCs and delivery vehicles travel from/to DCs to service customers. In the upper echelon of the network products flow from factories or central warehouses to DCs. Thus, such a company may consolidate shipments in both stages of the network. Different modes of transportation may be used for bulk transportation from upper echelon facilities.

By nature, LSPs offer services to many companies. Depending on their yearly contracts, the same DC may be used for more than one customer. This type of consolidation brings out the importance of warehouse management activities. Hence, the costs of operating DCs may grow with increasing capacity utilization.

Usually, the type of service offered by such a company is one-way: from the plant or DC towards the customers. This results in empty vehicles returning to the DCs. Providing service to more than one company may actually help in filling vehicles on their return trips. An LSP company usually works with a fleet of vehicles which are not dedicated to any DC or customer zone. Depending on the origin and destination of the demand, vehicles are assigned dynamically.

LSP companies often choose to specialize their services based on the sector of activity of their customers. Some examples include service providers for the automotive industry or the cold chain, parcel delivery companies, etc. The generic distribution network needs to be specialized depending on the application dynamics of the sector where the service provider operates. For example, for cargo delivery companies consolidation (hubbing) is very important in the design of the network (see e.g., Tan and Kara 2007, Yaman et al. 2007, and Alumur and Kara 2008).

### 16.4.3 Logistics Network Design for Organ Transportation

In this section, an atypical application of distribution logistics is discussed, namely the design of a network for organ transportation. Due to the nature of the “product” that flows through the network, this problem has specific features. It cannot be simply considered as a cold chain application, mainly because it is not possible to re-freeze and store organs. The organ which is harvested from a donor has to be implanted into the recipient’s body within the so-called ischemia time, which represents the time that an organ can be safely secured without fresh blood circulation. Thus, in this area, apart from logistics costs, delivering in a timely
manner is more important and so the logistics network is designed mainly based on delivery time requirements.

Since the organ cannot be stored, DCs or warehouses are not considered in the distribution network. Once an organ is donated, a search is conducted for the recipient with the best match and then the organ is transported to the hospital of the recipient. The most important aspect is to find the best match and send the organ in a timely manner so that the donated organ (which is definitely a very scarce resource) is not wasted. Search for potential recipients and organ transportation are under the jurisdiction of regional coordination centers (RCCs) operated by the government. Each RCC is responsible for a region, and any organ donated to an RCC is usually transferred into a recipient’s body in the same region.

In this context, the LND problem consists of finding the best locations for RCCs so that the regions covered by them are balanced in terms of their donor-recipient ratio and the transportation of organs in each region is possible within the ischemia time. For this type of networks, donors represent the supply side and the hospitals performing organ transplants (and where the recipients are registered) are the demand points. Examples of this type of centralized organ transportation networks include Bruni et al. (2006), Kong et al. (2010), Beliën et al. (2013), and Çağ and Kara (2014). We remark that in this application area the location of an RCC mainly determines a region. Shipment consolidation at an RCC is not allowed since the transportation of an organ from a donor to a recipient is a dedicated trip carried out, for example, by helicopter.

### 16.4.4 Reverse Logistics Network Design for Waste Electrical and Electronic Equipment

The Waste Electrical and Electronic Equipment (WEEE) Directive of the European Commission (2002/96/EC) sets collection, recovery, and recycling targets for all types of electrical and electronic goods. The achievement of the targets for each product category is calculated according to the total amount of WEEE that goes through specific recovery options. Original equipment manufacturers are held responsible for financing the collection, treatment, recovery, and disposal of their products.

The Directive enforces a separate collection for WEEE. For this purpose, appropriate facilities should be set up for collection. These facilities accumulate the returns, either dropped off by the product holders or picked up by the collectors. After collection, the returns can be sent to recycling and proper disposal, or to inspection and disassembly centers. The inspected products can be disassembled into components in these centers or sold to external facilities. The returns that are deemed non-remanufacturable through inspection are recycled or disposed of. In the event that the original equipment manufacturer decides to establish remanufacturing
facilities, then suitable components can be re-used in such facilities to obtain new products that can be sold to the secondary market.

The RLND problem under the WEEE Directive focuses on determining the locations and capacities of collection and inspection centers, on deciding if it is profitable to establish remanufacturing facilities, on setting the amount of products or components to send to different recovery options, to recycling and disposal, and on fixing the flow of products and components through the facilities in the network (see e.g., Alumur et al. 2012).

16.5 Conclusions

This chapter highlighted the importance of integrating location decisions with other decisions relevant to the design of forward and reverse logistics networks. Although much work has been published addressing LND problems, emphasis has been mostly given to a subset but not all of the features that such comprehensive projects often require. Hence, several research directions still require intensive research. In particular, models addressing the design of multi-commodity, multi-echelon networks through determining the timing of facility locations, expansions, contractions, and relocations over an extended time horizon have received less attention than their static counterpart.

Traditionally, LND has been dominated by economic aspects leading to the network configuration that either minimizes total cost or maximizes total profit. The generic models presented in Sects. 16.2.2 and 16.3.2 illustrate these features. Sustainable LND is an emerging research area that aims at capturing the trade-offs between costs on facility location and logistics functions and their environmental footprint. Due to the growing awareness on environmental issues, companies have recognized the need to create environmentally friendly logistics systems to mitigate the negative environmental impact of their business activities. This calls for the development of models with multiple and conflicting objectives. For example, Chaabane et al. (2012) formulate a bi-objective LND model involving the minimization of network design costs and the minimization of green gas emissions. The latter criterion is part of a longer list of environmental factors that should be considered, according to Chen et al. (2014), together with social and economic factors when deciding on the location of manufacturing facilities.

Humanitarian logistics has also become a new research field involving LND. Döyen et al. (2012) integrate facility location decisions with transportation, inventory management, and shortage policies in a two-echelon model. Uncertainty on the location and intensity of a natural disaster is explicitly incorporated into the model. The integration of different sources of uncertainty (e.g., customer demand, product return in the context of reverse logistics) with network design decisions is also a research direction requiring further attention.

Finally, it goes without saying that LND has given rise and will continue to provide a rich variety of problems. LND presents a challenging area for future research.
on the development of mathematical models and optimization methodologies. More and more organizations recognize the importance of an efficient and agile logistics network for responding to changes in the business environment and enabling future growth. Therefore, LND will play an even greater role for companies in all industries striving to deliver outstanding supply chain performance.

References


